

# Mechanics of carbon nanotubes and their polymer composites

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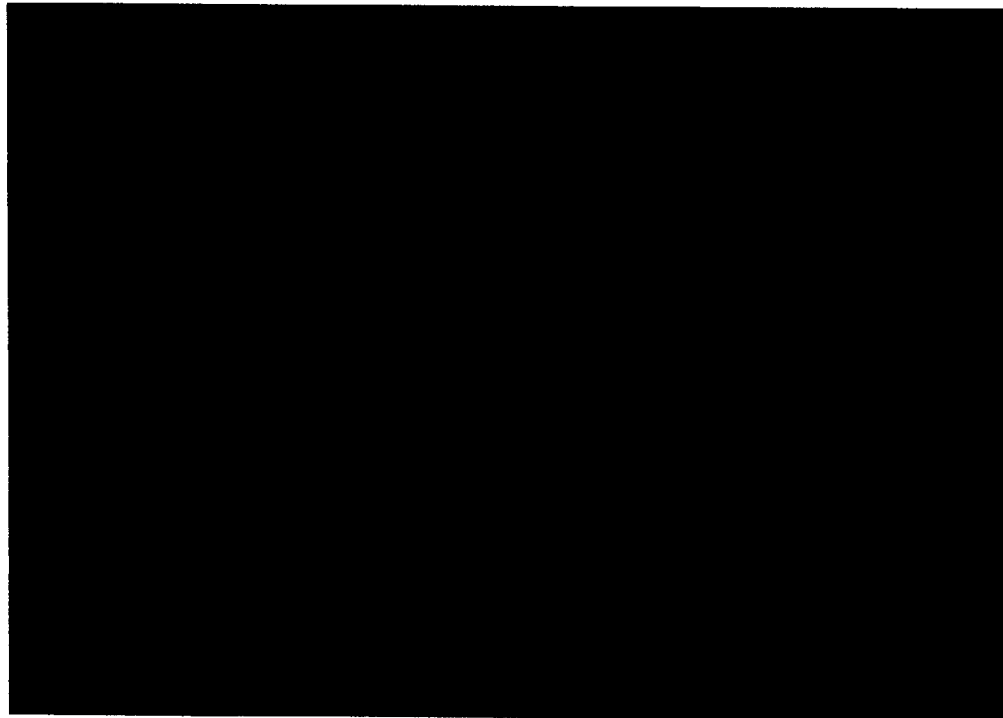
*Collaboration With KJ Cho (Stanford University, CA)  
and Deepak Srivastava (NASA Ames Research center, CA)*

## Carbon Nanotube: Structures

*Atomic structure:*

Quasi one dimensional; C-C bond length 1.43 Å;

Radius ~ Nanometer; Length ~  $\mu\text{m}$  (current upper range); Index (n,m)



## Application of Carbon Nanotubes

*Nano fibers:* Strong mechanical properties

*Nano devices:* Wide variety of electronic properties and mechanical-electronic couplings

*Nano sensors:* Physical and Chemical adsorption of gas molecules, ions

## Simulation Methods

### (1) **Molecular Dynamics:** Newton's Equation

Force Field for Carbon nanotubes:

*Tersoff Brenner potential*, fitted to carbon and hydrocarbon systems, 3-body type, bond broken and formation

### (2) Tight Binding method

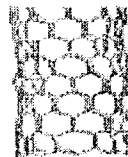
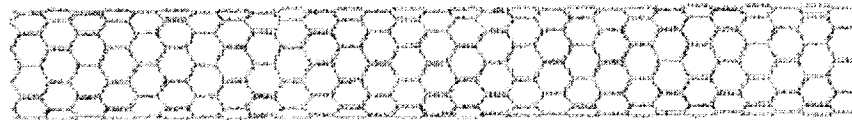
### (3) Ab initio method (Density Functional theory)

# Elastic Properties of Carbon Nanotubes

Small strain: uniform deformations, elastic behavior  
continuum theory applicable

Large strain: local deformations, defects, dislocations

Tension, Compression, bending, and (Torsion):



## Yield Strain of CNT

### Tension

*Simulation:* 30% yield strain from fast strain rate (1/ps) molecular dynamics simulations (B.I. Yakobson et.al. Comput. Mater. Sci. 1997 )

*Experiments:* 6% maximum strain in SWCNT ropes; 12% maximum strain in MWCNTs (D.A. Walter et al, Appl. Phys. Lett. 1999; M.F. Yu et al, Phys. Rev. Lett. and Science 2000)

### Compression

*Simulation:*

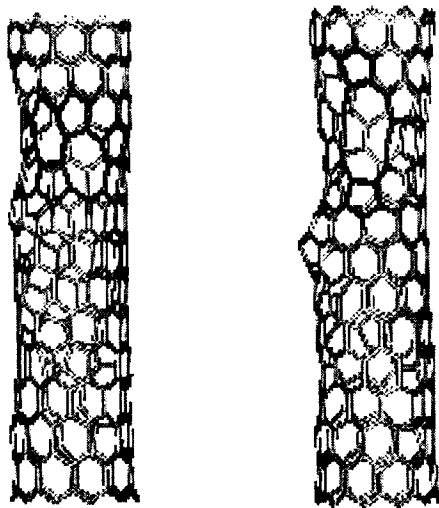
T=0K, Tersoff-Brenner potential: Super-elastic up to 20%

T=0K, Tight Binding: diamond like defects, collapsed at 12%

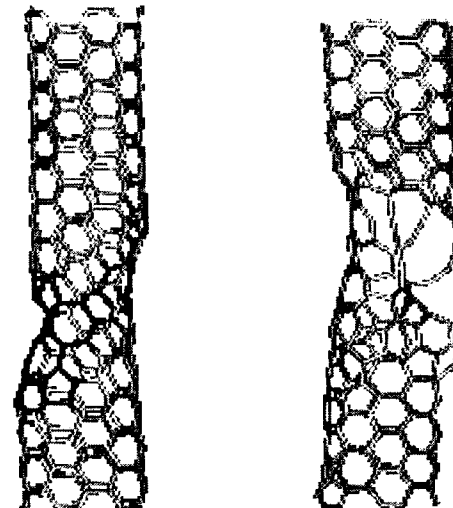
*Experiment:*

Collapsing of CNT within polymer matrix under compression stress 150GPA (TEM study)

## Yielding under Tensile Stress



11.5% tensile strained  
CNT (10,0),  $T=1600\text{K}$

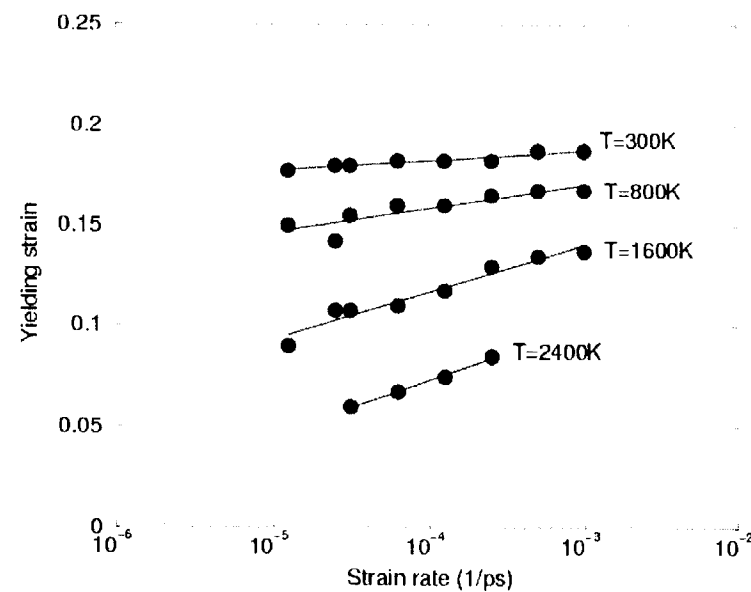
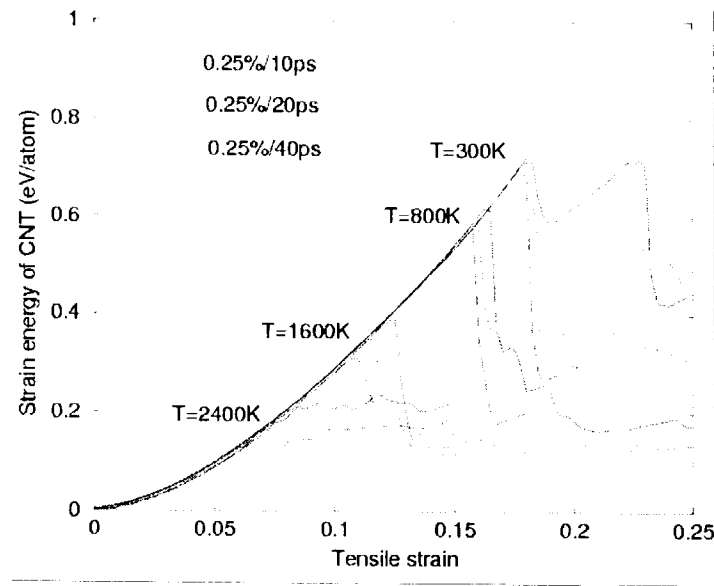


9% tensile strained  
CNT (5,5),  $T=2400\text{K}$

\* D. Srivastava, C. Wei, and K. Cho, Appl. Mech. Review (2002)

# Yielding: Strain-rate and Temperature Dependence

Tensile strain applied to a 60Å long (10,0) CNT



- Yielding: strongly dependent on strain rate and Temperature
- Linear dependent on temperature of the slope of yield strain vs. strain rate : Activated Process



## Yield Strain under Tension

$$\varepsilon_Y = \frac{\bar{E}_v}{VK} + \frac{k_B T}{VK} \ln\left(\frac{N \dot{\varepsilon}}{n_{\text{site}} \dot{\varepsilon}_0}\right)$$

$\dot{\varepsilon}$  : Strain rate;  $\dot{\varepsilon}_0$  : Constant related with vibrational frequency

$K$  : Force constant;  $V$ : Activation volume;  $\bar{E}_v$ : Activation energy

$N$  : Number of process involving in yielding;  $n_{\text{site}}$  : Site available

Length effect:

$$\Delta \varepsilon_Y = -\frac{k_B T}{VK} \ln(n_{\text{site}}/n_{\text{site}}^0)$$

Temperature effect:

$$\left(\frac{\dot{\varepsilon}_1 N}{n_{\text{site}} \dot{\varepsilon}_0}\right)^{T_1} = \left(\frac{\dot{\varepsilon}_2 N}{n_{\text{site}} \dot{\varepsilon}_0}\right)^{T_2}$$

## Yielding at Realistic Conditions

- *Parameters obtained from fitting of MD simulations' data*

$$\bar{E}_v = 3.6\text{eV}; \quad V = 2.88 \text{ \AA}^3$$

$$\frac{\dot{\epsilon}_0}{N} = 8 \times 10^{-3} \text{ p s}^{-1}$$

- *Experimental feasible conditions*

length  $\sim 1\mu\text{m}$ ; strain rate  $\sim 1\%/ \text{hour}$ ;  $T \sim 300\text{K}$

$\Rightarrow$  Yield strain:  $9 \pm 1 \%$

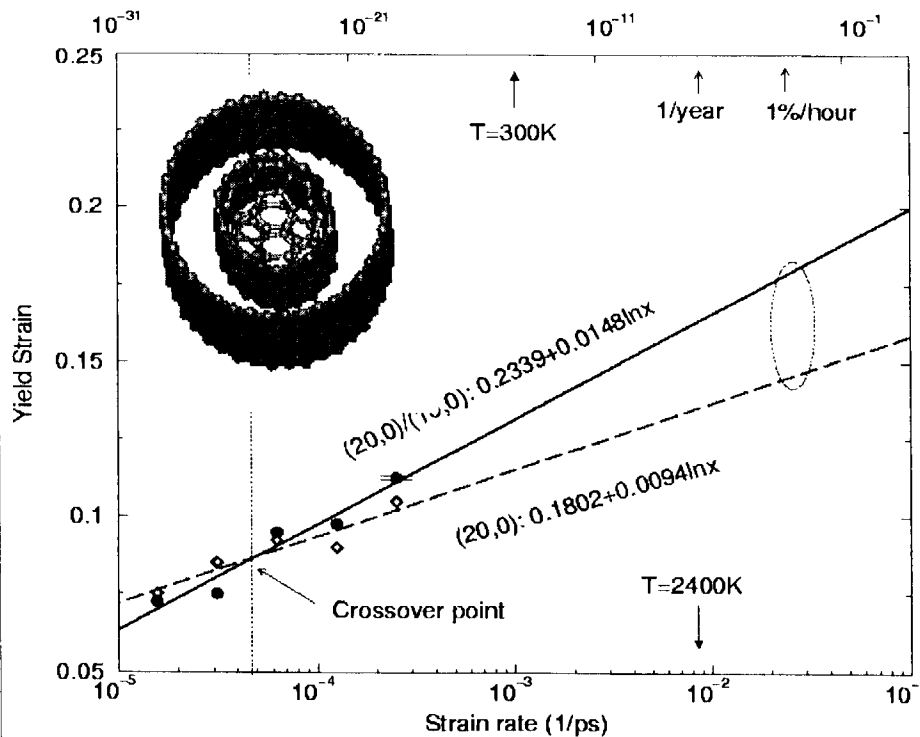
Maximum tensile strains from experiments:

5-6 % for SWCNT ropes; 12% for MWCNTs

\* D.A. Walter, et. al. , Appl. Phys. Lett. V74, 3803 (1999)

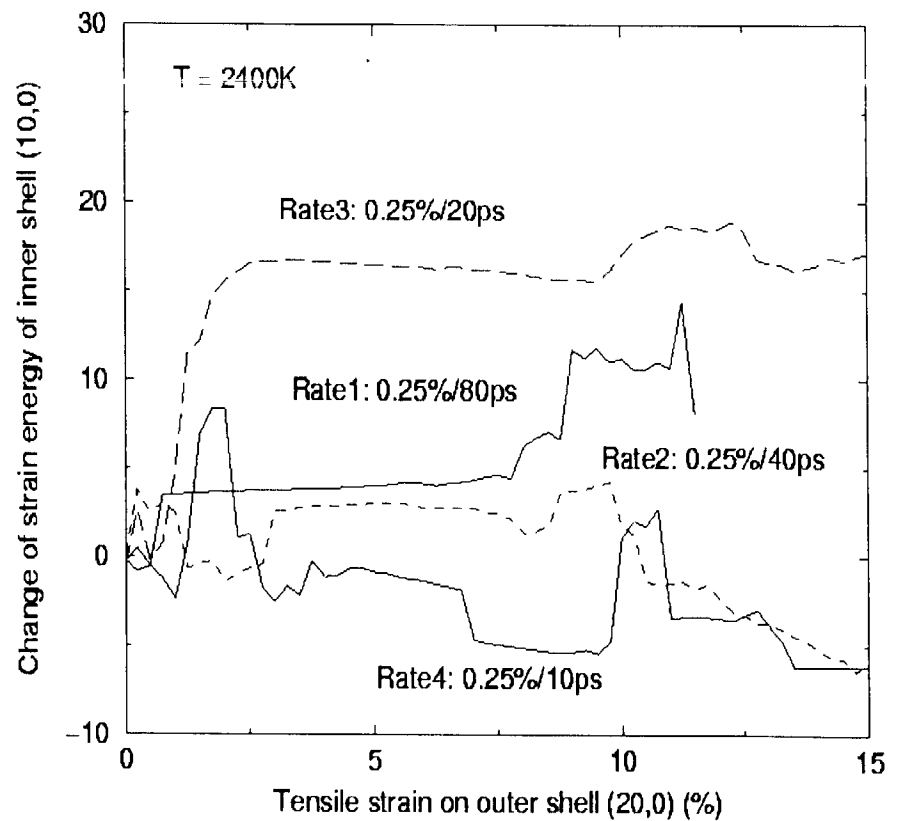
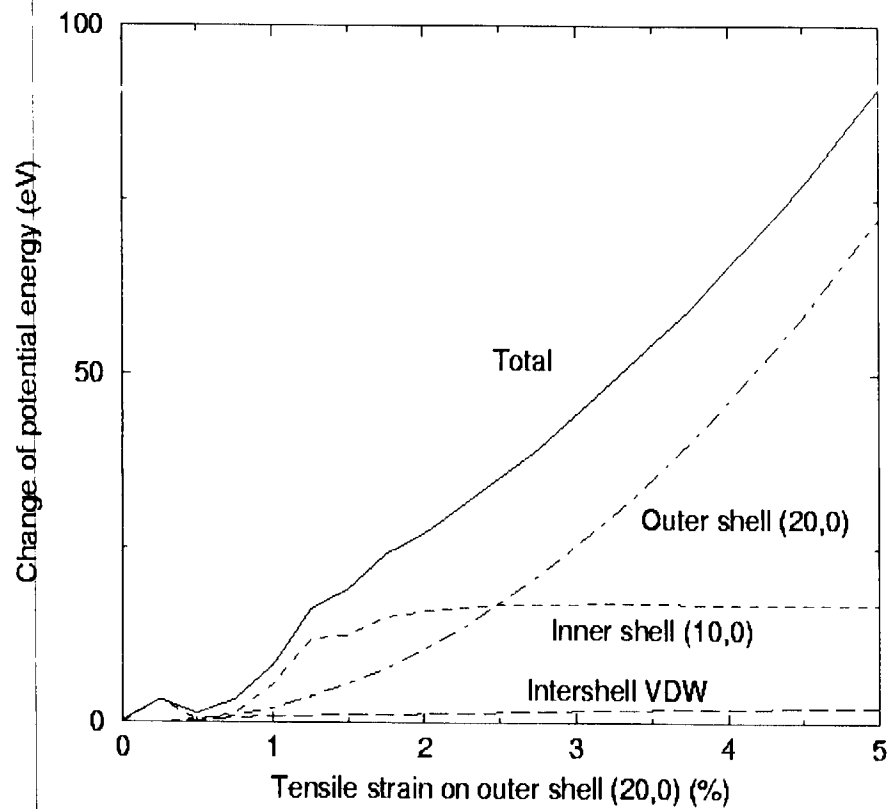
M.-F. Yu et.al. Phys. Rev. Lett., V84, 5552 (2000); M.-F. Yu et. al., Science, V287, 637 (2000)

## Yielding of MWCNT



- (1) For  $\dot{\epsilon} = 1\%/hour$ , and  $T=300K$   
 $\epsilon_Y$  (MWCNT) > (SWCNT): 3-4%;
- (2) Activation volume on MWCNT is smaller (60%-70% of that on SWCNT);
- (3) Crossover point of strain rate exponentially dependent on  $T$ , important for high temperature situations.

## Load transfer on MWCNT



## CNT: Nano Fibers

### *CNT to reinforce composites*

- High Strength & High flexibility & Toughness & light-weight (Young's Modulus > 1 TPa)
- High aspect ratio  $L/D$ , can reach 1000  
Critical length:  $L_c/D \sim \sigma_{\max}/2\tau$ 
  - $L_c$ : length of CNT;  $D$ : diameter of the CNT;
  - $\sigma_{\max}$ : tensile strength of CNT;
  - $\tau$ : interfacial shear stress
- Large surface area, good for bonding, adhesion

## Polymer-CNT Composite

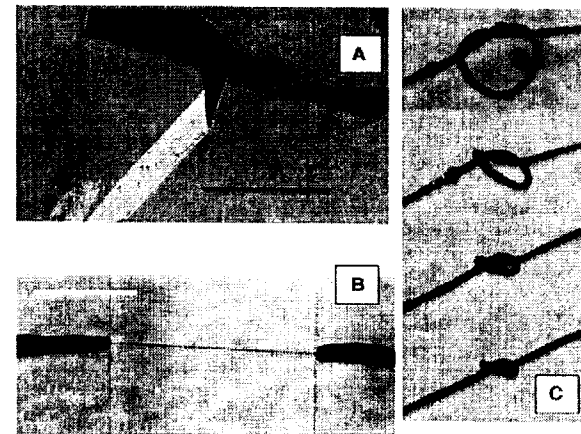
- *Structural and thermal properties*
- *Load transfer and mechanical properties*

SEM images of epoxy-CNT composite



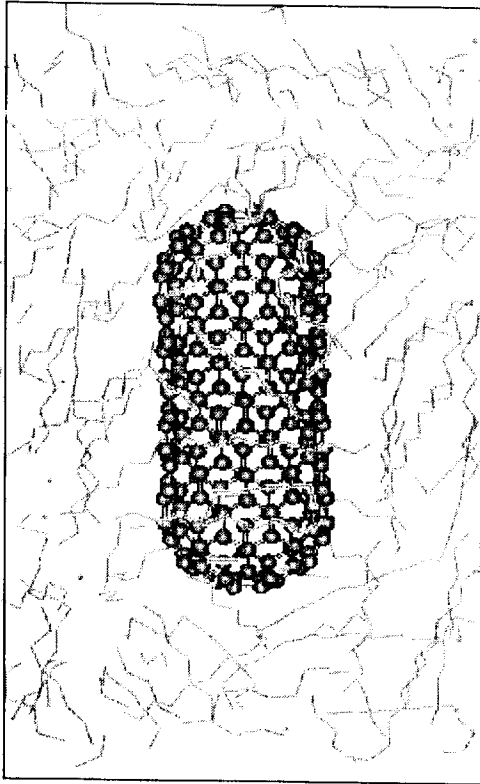
(L.S.Schadler et.al., Appl. Phys. Lett. V73 P3842, 1998)

SEM images of CNT fibers ribbon  
(processing in polyvinylalcohol solution) &  
knotted CNT fibers



(B. Vigolo et.al., Science, V290 P1331, 2000)

# MD Simulations of Polymer-CNT



Polymer-CNT composite

## Simulation method

*Classical MD*: Tersoff-Brenner potentials for CNT, DLPOLY for polymer, and VDW interactions

## System in simulation

*Polyethylene & (10,0) CNT* : (80 chains of PE relaxed by Monte Carlo methods,  $N_p=10$ ; 20Å long CNT 8% volume ratio)

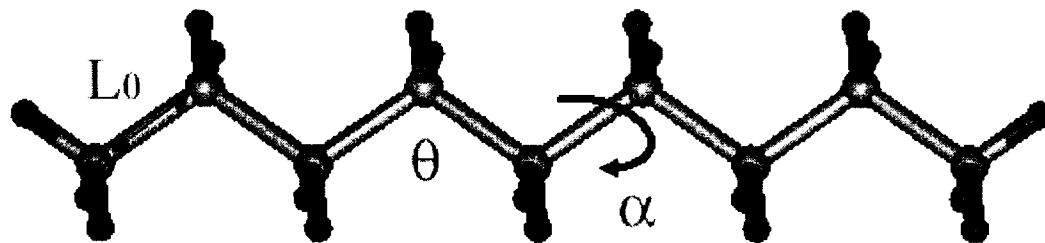
## Preparations

Composites prepared at 300K; cooled down to 10K with rate 1K/1ps

composites change from liquid state through rubber state to glassy state

## Force Field

### *Intramolecular potentials*



Valence angle potential:  $\Phi(\theta) = 0.5k_{\theta}(\cos \theta - \cos \theta_0)^2$ ,

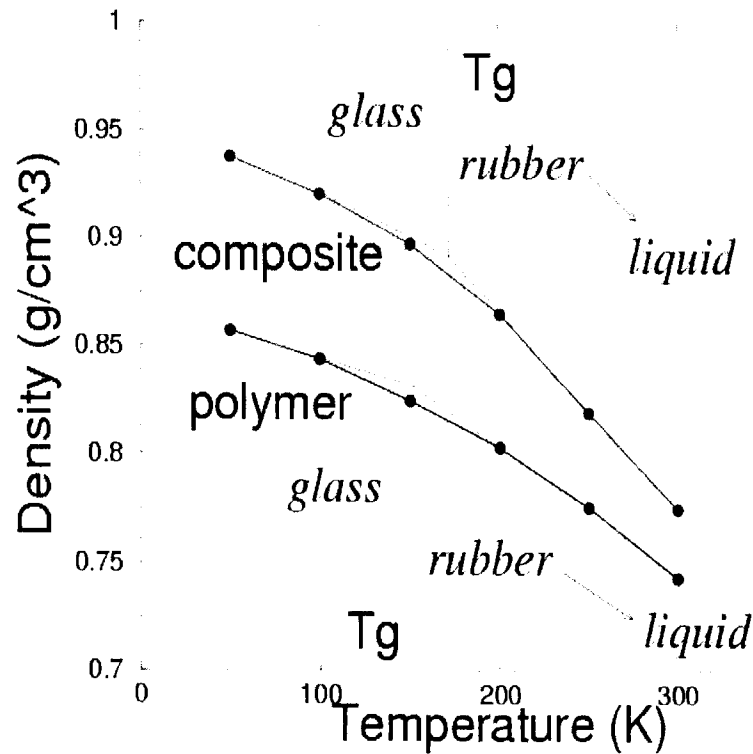
Torsion potential:  $\Phi(\alpha) / \text{J} \cdot \text{mol}^{-1} = C_0 + C_1 \cos \alpha + C_2 \cos^2 \alpha + C_3 \cos^3 \alpha$ ,

Harmonic potential:  $0.5 k_b (l - l_0)^2$



# Density Dependence on Temperature

Small system:  $L/D \sim 2$ ,  $N_p = 10$



## Results

-Glass transition temperature  $T_g$  increased from 150K to 175K

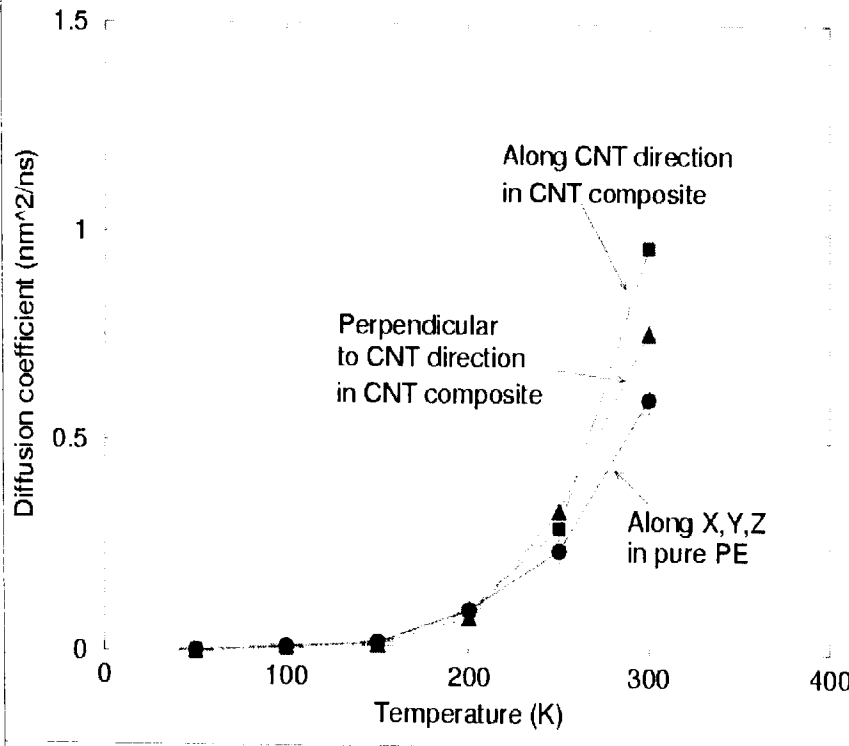
-Thermal expansion coefficients: ( $K^{-1}$ )

	PE	PE-CNT	
$T < T_g$	$3.8 \times 10^{-4}$	$4.5 \times 10^{-4}$	$\uparrow 18\%$
$T > T_g$	$8.6 \times 10^{-4}$	$12.0 \times 10^{-4}$	$\uparrow 40\%$

(Experimental value:  $1.0 \times 10^{-4} K^{-1}$ ;  $T < T_g$ )

# Diffusion Coefficients

Small system:  $L/D \sim 2$ ,  $N_p = 10$



Diffusion coefficients of polymer with CNTs embedded

Diffusion coefficient increased, especially along CNT axis direction, indicating enhancement of thermal conductivity

- Experiments on ABS/CNT & RTV/CNT show larger increase (Rick Berrera's group at RICE)

(Ajayan's group at R.P.I. is investigating these subjects in detail)

\* C. Wei, D. Srivastava, and K. Cho (Nano Letters, in press)

# Modulus of Polymer-CNT Composites

(Halpin-Tsai's formula)

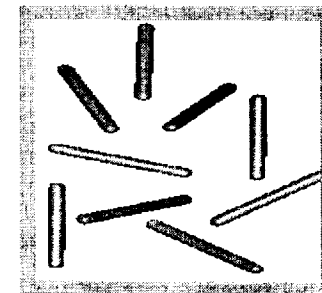
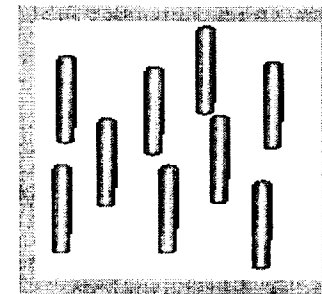
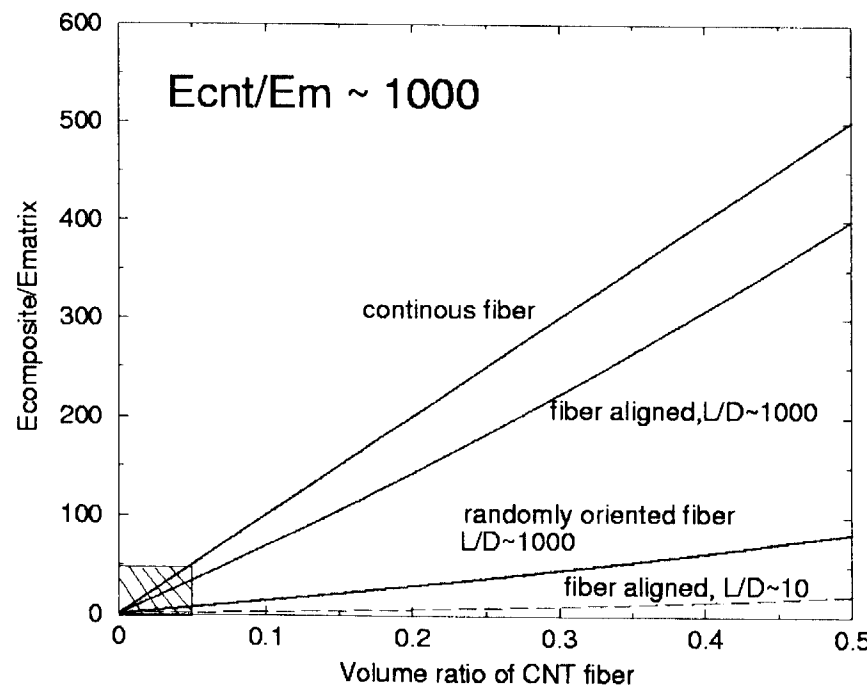
$$\frac{E_c}{E_m} = \frac{1 + \xi \eta V_f}{1 - \eta V_f}$$

$E_c, E_m, E_f$ : Modulus of composite, matrix and fiber

$V_f$ : Volume ratio of fiber

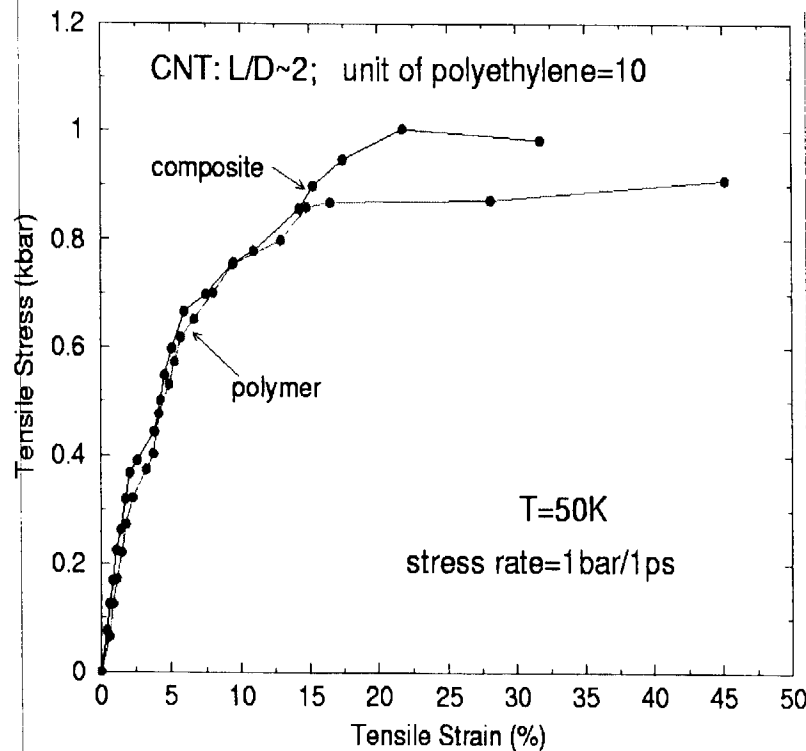
$$\eta = \frac{(M_f / M_m - 1)}{(M_f / M_m + \xi)}$$

$\xi$ : Dependent on geometry, packing of fiber; aspect ratio of fiber



# Stress-Strain Curve & Load Transfer

Mechanical behavior of Composite:  
Elastic region and Yielding



Enhancement of Young's modulus: 30%

Load transfer: within 0.7%

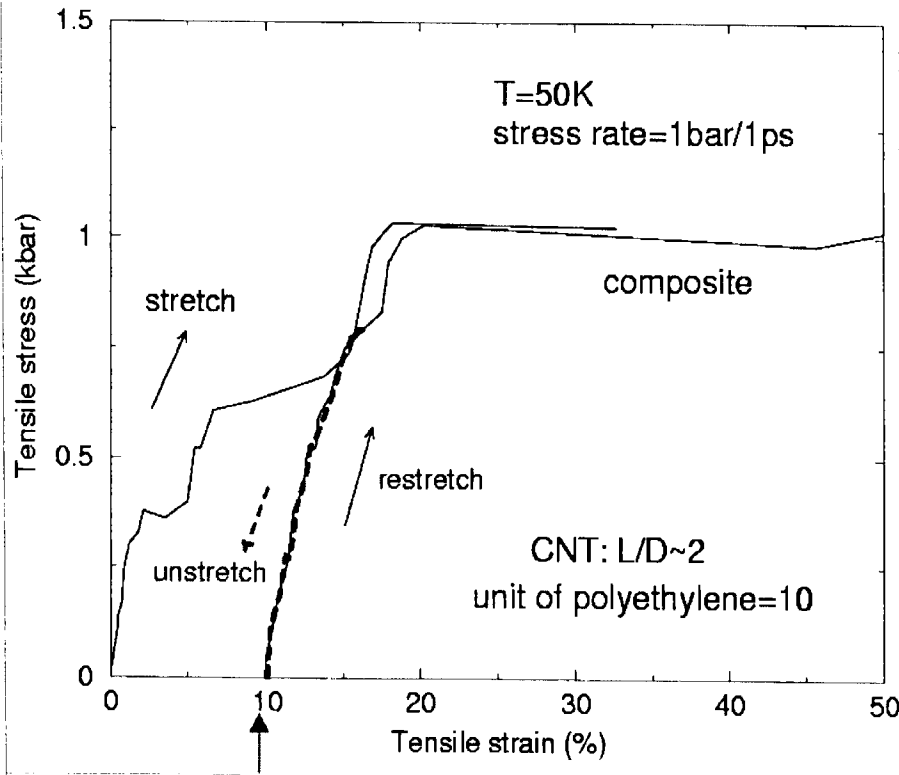
Poisson Ratio effect:

CNT  $\sim 0.1-0.2$ , Polyethylene  $\sim 0.44$

Compression pressure perpendicular to tube axis contribute to improvement

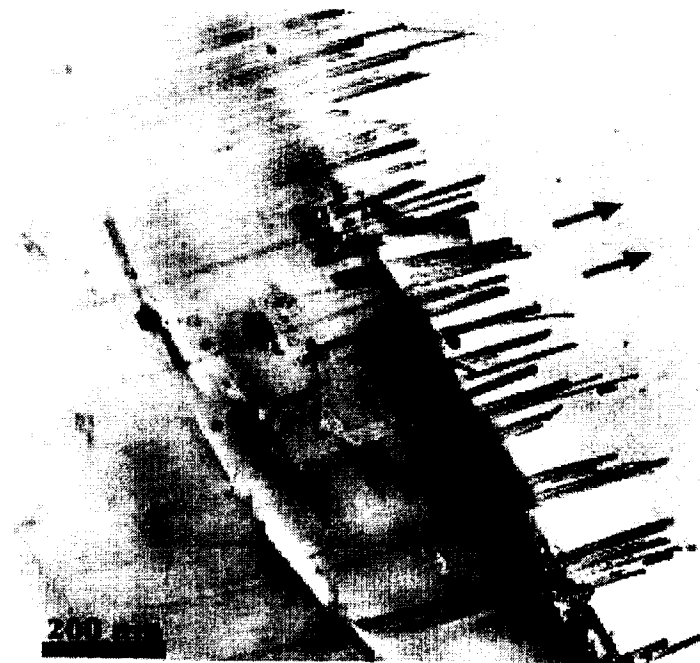
## Loading Sequence

Work hardening of composite  
with stretching



•Residue strain

TEM images of alignment of CNTs  
in a polymer matrix by stretching



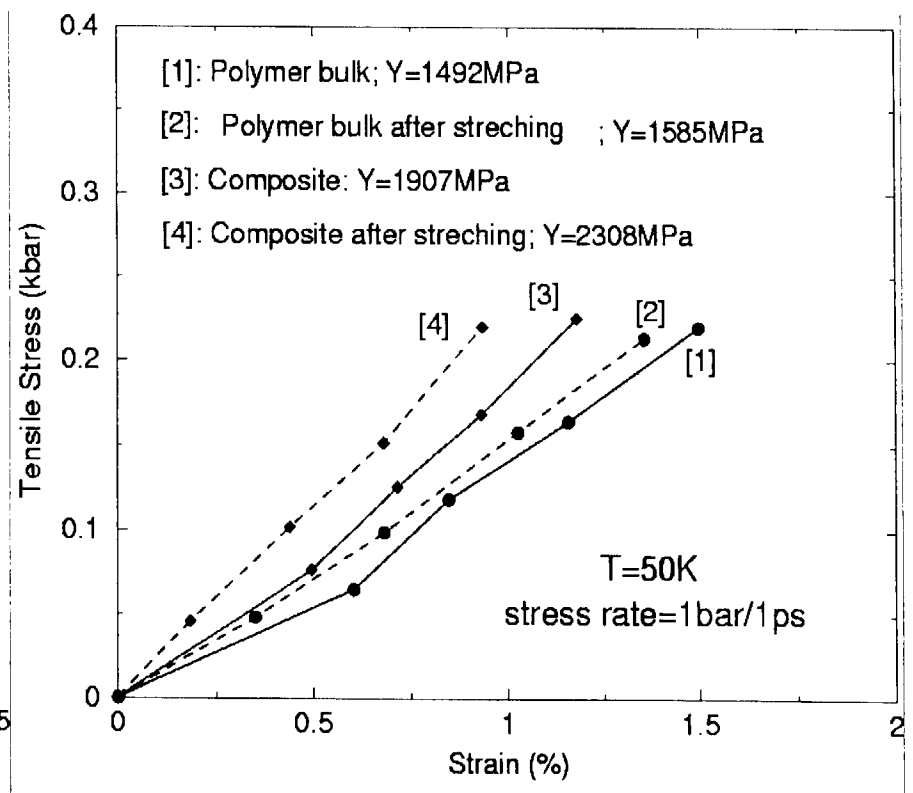
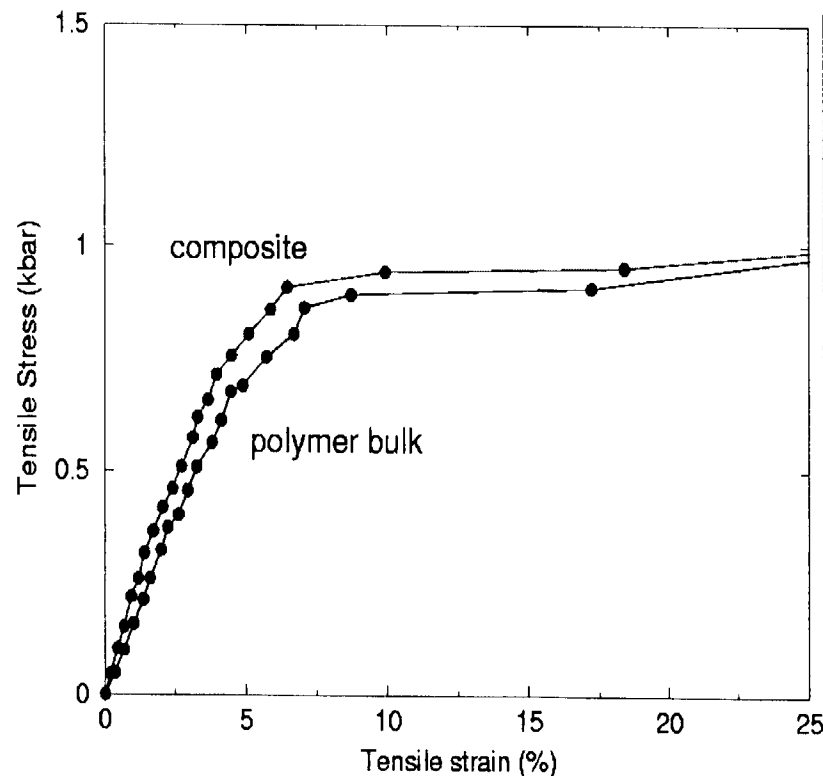
(L. Jin et.al., Appl.Phys. Lett., V73 P1197, 1998)

# Young's Modulus

-Young's modulus of CNT composites 30% higher than polymer matrix

-Stretching treatments enhance Y by 50%

( $L/D \sim 2$ ,  $N_p = 10$ )



## Conclusions

- Yielding of carbon nanotubes strongly dependent on strain rate and temperature: transition state theory
- Polymer-CNT composite has larger thermo-expansion above  $T_g$ 
  - Phonon modes and Brownian motion leading to larger exclude volume of embedded CNT
  - Diffusion of polymer matrix increased above  $T_g$
- Young's modulus of composite enhanced by 30% through VDW interaction.
  - Load transfer happening within 0.7%; stiffness of CNT bond increases modulus of composite
  - Loading sequence can improve the enhancement of modulus of composite